

EE321 Sixth Homework Assignment

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1 Fourier Transforms

1. Find Fourier transforms of the following functions

(a) $f_1(t) = 3e^{-3t}u(t - 2)$

(b) $f_2(t) = e^{-2t}[u(t) - u(t - 2)]$

(c) $f_3(t) = 2\text{rect}(\frac{t-5}{2})$

(d) $f_4(t) = \text{rect}(\frac{t+1}{2}) + \text{rect}(\frac{t-1}{2})$

(e) $f_5(t) = f_4(2t)$

(f) $f_6(t) = 2 \sin c(4\pi t)$

(g) $f_7(t) = f_2(t - 2)$

(h) Given Fourier transforms of $\delta(t)$ is 1, use Fourier transforms duality and frequency shift properties to prove that Fourier transform of $e^{j\omega_0 t}$ is $2\pi\delta(\omega - \omega_0)$.

(i) $f_8(t) = \text{rect}(\frac{t}{T}) \cos(\omega_0 t)$

(j) $f_9(t) = t[u(t - 1) - u(t - 5)]$

2. Find inverse Fourier transform of the following functions:

(a) $F_1(\omega) = \text{rect}(\frac{2\omega-6\pi}{4})$

(b) $F_2(\omega) = 3e^{-2a|\omega|}$

(c) $F_3(\omega) = 4 \cos(\tau\omega)$

(d) $F_4(\omega) = 3 \sin c(5\omega)$

3. Sketch the following functions:

(a) $f(t) = 2 \cdot \text{sinc}(\frac{2\pi t-2}{6\pi})$

(b) $F(\omega) = \text{rect}(\frac{2\omega-6\pi}{4})$

4. A system transfer function is $H(s) = s^2 + 5s + 4$ and input signal is $x(t) = 2 \cos(20\pi t)$ using the convolution property of the Fourier transform to

(a) find the Fourier transform of the output signal $y(t)$, and

(b) Sketch the magnitude and phase spectrum. (hint: $F(\omega) \cdot \delta(\omega - \omega_0) = F(\omega_0) \cdot \delta(\omega - \omega_0)$)

(c) Can you tell the steady state response $y_{ss}(t)$ from the above answers and what is it?

5. Given Fourier transform of a continuous-time signal $x(t)$ is

$$X(j\omega) = \frac{A}{j\omega + p}$$

find Fourier transforms of

(a) $f(t) = 3x(2t - 4)$

(b) $y(t) = \frac{d^2x(t)}{dt^2}$

(c) $w(t) = t^2x(t)$

(d) $v(t) = x(t) \cos(3t)$

(e) $q(t) = x(t) * x(t)$ where $*$ is linear convolution

6. Find the Fourier transform of the following periodic signal and show that it is equivalent

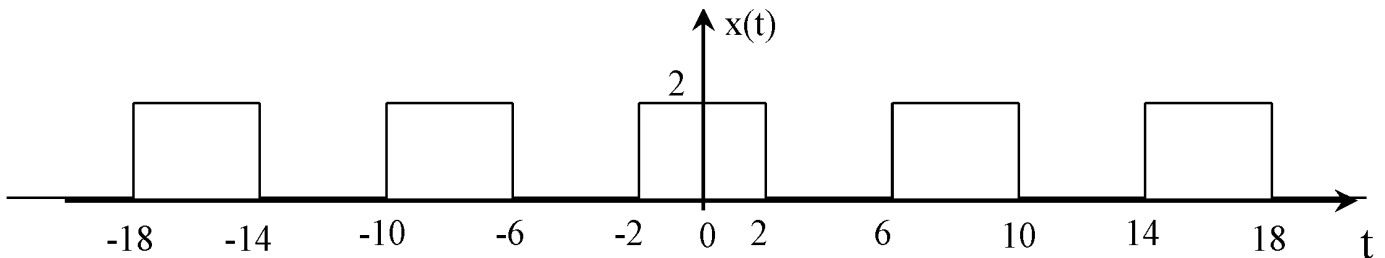


Figure 1:

to the Fourier series coefficients D_n .

7. **Extra exercise problems in the text book:** 4.6-1 and 4.6-5