

PROB. 13-155

$$\vec{v}_A = (2) \hat{i} \frac{\text{m}}{\text{s}}, \quad \vec{v}_B = (-1.5) \hat{i} \frac{\text{m}}{\text{s}}, \quad m_A = 5 \text{ kg}, \quad m_B = 3 \text{ kg}$$
$$e = 0.80$$

a) FIND VELOCITIES AFTER IMPACT

CONSERVATION OF MOMENTUM:

$$m_A \vec{v}_A + m_B \vec{v}_B = m_A \vec{v}_A' + m_B \vec{v}_B'$$

$$(5 \text{ kg}) \left(2 \frac{\text{m}}{\text{s}} \right) + (3 \text{ kg}) \left(-1.5 \frac{\text{m}}{\text{s}} \right) = (5 \text{ kg}) v_A' + (3 \text{ kg}) v_B'$$

$$v_A' = \frac{1}{5} (5.5 - 3 v_B') = 1.1 - 0.6 v_B'$$

COEFFICIENT OF RESTITUTION:

$$v_B' - v_A' = e (v_A - v_B) = (0.8) \left[(2) - (-1.5) \frac{\text{m}}{\text{s}} \right] = 2.8$$

$$v_B' - (1.1 - 0.6 v_B') = 2.8$$

$$\boxed{v_B' = 2.437 \frac{\text{m}}{\text{s}}} \quad \boxed{v_A' = 1.1 - 0.6(2.437) = -0.3625 \frac{\text{m}}{\text{s}}}$$

b) FIND ENERGY LOSS DURING IMPACT

$$(T_A + T_B) = \frac{1}{2} m_A v_A^2 + \frac{1}{2} m_B v_B^2 = \frac{1}{2} \left[(5 \text{ kg}) \left(2 \frac{\text{m}}{\text{s}} \right)^2 + (3 \text{ kg}) \left(1.5 \frac{\text{m}}{\text{s}} \right)^2 \right]$$
$$= 13.37 \text{ N}\cdot\text{m}$$

$$(T_A + T_B)' = \frac{1}{2} m_A (v_A')^2 + \frac{1}{2} m_B (v_B')^2$$
$$= \frac{1}{2} \left[(5) (0.3625)^2 + (3) (2.437)^2 \right] = 9.237 \text{ N}\cdot\text{m}$$

$$\boxed{\Delta T = 4.133 \text{ N}\cdot\text{m}}$$