

PROB. 15-135

$$\omega_{AB} = 4 \frac{\text{RAD}}{\text{s}} \curvearrowright, \quad \alpha_{AB} = 2 \frac{\text{RAD}}{\text{s}^2} \curvearrowright, \quad \omega_{ED} = -6.4 \frac{\text{RAD}}{\text{s}},$$
$$\omega_{BD} = -5.2 \frac{\text{RAD}}{\text{s}} \curvearrowright \quad \text{FIND } \alpha_{BD}, \alpha_{DE}$$

ACCELERATION

$$\vec{a}_B = \vec{a}_A + \alpha_{AB} \hat{k} \times \vec{r}_{B/A} - \omega_{AB}^2 \vec{r}_{B/A}$$

$$\alpha_{AB} \hat{k} \times \vec{r}_{B/A} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 0 & -2 \\ -0.4 & -0.8 & 0 \end{vmatrix}$$

$$= [0 - (-2)(-0.8)] \hat{i} - [0 - (-2)(-0.4)] \hat{j}$$

$$= (-1.6) \hat{i} + (0.8) \hat{j} \frac{\text{m}}{\text{s}^2}$$

$$-\omega_{AB}^2 \vec{r}_{B/A} = -(-4)^2 [(-0.4) \hat{i} + (-0.8) \hat{j}]$$

$$= (6.4) \hat{i} + (12.8) \hat{j}$$

$$\vec{a}_B = (-1.6) \hat{i} + (0.8) \hat{j} + (6.4) \hat{i} + (12.8) \hat{j}$$

$$\vec{a}_B = (4.8) \hat{i} + (13.6) \hat{j} \frac{\text{m}}{\text{s}^2}$$

$$\vec{a}_D = \vec{a}_B + \alpha_{BD} \hat{k} \times \vec{r}_{D/B} - \omega_{BD}^2 \vec{r}_{D/B}$$

$$\alpha_{BD} \hat{k} \times \vec{r}_{D/B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 0 & \alpha_{BD} \\ 0.8 & 0 & 0 \end{vmatrix} = -[0 - (\alpha_{BD})(0.8)] \hat{j}$$

$$= (0.8 \alpha_{BD}) \hat{j} \frac{\text{m}}{\text{s}^2}$$

PROB. 15-135 CONT.

$$-\omega_{BD}^2 \vec{r}_{D/B} = -(-5.2)^2 (0.8) \hat{i} = (-21.63) \hat{i} \frac{m}{s^2}$$

$$\vec{a}_D = (4.8) \hat{i} + (13.6) \hat{j} + (0.8 \alpha_{BD}) \hat{j} + (-21.63) \hat{i}$$

$$\vec{a}_D = (-16.83) \hat{i} + (13.6 + 0.8 \alpha_{BD}) \hat{j} \frac{m}{s^2}$$

$$\vec{a}_D = \vec{a}_E + \alpha_{DE} \hat{k} \times \vec{r}_{D/E} - \omega_{DE}^2 \vec{r}_{D/E}$$

$$\alpha_{DE} \hat{k} \times \vec{r}_{D/E} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 0 & \alpha_{DE} \\ 0.4 & -0.5 & 0 \end{vmatrix}$$

$$= [0 - (\alpha_{DE})(-0.5)] \hat{i} - [0 - (\alpha_{DE})(0.4)] \hat{j}$$

$$= (0.5 \alpha_{DE}) \hat{i} + (0.4 \alpha_{DE}) \hat{j} \frac{m}{s^2}$$

$$-\omega_{DE}^2 \vec{r}_{D/E} = -(-6.4)^2 [(0.4) \hat{i} + (-0.5) \hat{j}]$$

$$= (-16.38) \hat{i} + (20.48) \hat{j} \frac{m}{s^2}$$

$$\vec{a}_D = (0.5 \alpha_{DE}) \hat{i} + (0.4 \alpha_{DE}) \hat{j} + (-16.38) \hat{i} + (20.48) \hat{j}$$

$$\vec{a}_D = (0.5 \alpha_{DE} - 16.38) \hat{i} + (0.4 \alpha_{DE} + 20.48) \hat{j}$$

$$(-16.83) \hat{i} + (13.6 + 0.8 \alpha_{BD}) \hat{j} = (0.5 \alpha_{DE} - 16.38) \hat{i} + (0.4 \alpha_{DE} + 20.48) \hat{j}$$

$$X\text{-DIRECTION: } -16.83 = 0.5 \alpha_{DE} - 16.38 \Rightarrow \boxed{\alpha_{DE} = -0.9 \frac{RAD}{s^2}}$$

$$Y\text{-DIRECTION: } 13.6 + 0.8 \alpha_{BD} = 0.4(-0.9) + 20.48$$

$$\boxed{\alpha_{BD} = 8.15 \frac{RAD}{s^2}}$$