

PROB. 17-6

$$\omega_0 = \left(360 \frac{\text{REV}}{\text{MIN}}\right) \left(\frac{\text{MIN}}{60 \text{ S}}\right) \left(\frac{2\pi}{\text{REV}}\right) = 12\pi \frac{\text{RAD}}{\text{S}}$$

$$U_{1-2} = -1500 \text{ ft}\cdot\text{lb}, \quad \omega_F = 0.95\omega_0 = 0.95 \cdot 12\pi \frac{\text{RAD}}{\text{S}}$$

a) FIND I

$$\text{WORK AND ENERGY: } T_1 + U_{1-2} = T_2$$

$$\frac{1}{2} I \omega_0^2 + U_{1-2} = \frac{1}{2} I \omega_F^2$$

$$I = \frac{2U_{1-2}}{\omega_F^2 - \omega_0^2} = \frac{2(-1500 \text{ ft}\cdot\text{lb})}{\left(0.95 \cdot 12\pi \frac{\text{RAD}}{\text{S}}\right)^2 - \left(12\pi\right)^2} = 21.65 \text{ ft}\cdot\text{lb}\cdot\text{S}^2$$

b) $M = 18 \text{ ft}\cdot\text{lb}$, FIND $\Delta\theta$ FOR $\omega_F = 360 \text{ RPM} = 12\pi \frac{\text{RAD}}{\text{S}}$

$$T_1 + U_{1-2} = T_2$$

$$\frac{1}{2} I \omega_0^2 + M \cdot \Delta\theta = \frac{1}{2} I \omega_F^2$$

$$\Delta\theta = \frac{I}{2M} (\omega_F^2 - \omega_0^2) = \frac{(21.65 \text{ ft}\cdot\text{lb}\cdot\text{S}^2)}{2(18 \text{ ft}\cdot\text{lb})} \left[\left(12\pi \frac{\text{RAD}}{\text{S}}\right)^2 - \left(0.95 \cdot 12\pi\right)^2 \right]$$

$$\Delta\theta = (83.33 \text{ RAD}) \left(\frac{\text{REV}}{2\pi}\right) = 13.26 \text{ REV}$$