

17-61

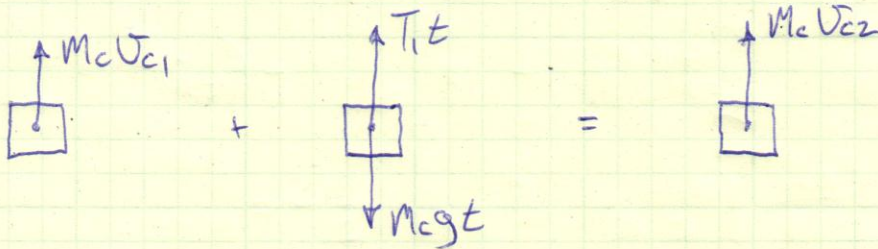
①

$r_A = 0.2 \text{ m}$, $r_B = 0.15 \text{ m}$, $m_A = 10 \text{ kg}$, $m_B = 6 \text{ kg}$, $m_C = 6 \text{ kg}$
 $m_D = 10 \text{ kg}$, STARTS FROM REST: FIND t FOR $v_{Cz} = 0.5 \frac{\text{m}}{\text{s}}$

SYSTEM WILL ROTATE CLOCKWISE.

PRINCIPLE OF IMPULSE AND MOMENTUM:

CYLINDER C:

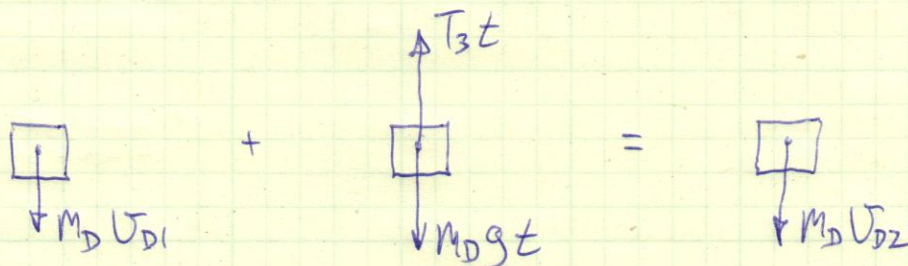


Y-DIR. LIN. MOM. $\uparrow +$:

$$m_C v_{C1} + T_1 t - m_C g t = m_C v_{C2}$$

$$T_1 t = m_C (g t + v_{C2}) \quad (1)$$

CYLINDER D:

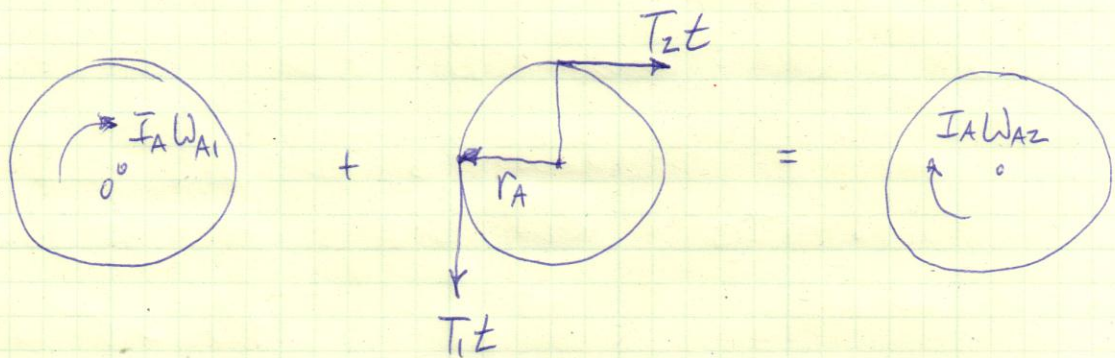


Y-DIR. LIN. MOM. $\downarrow +$:

$$m_D v_{D1} + m_D g t - T_3 t = m_D v_{D2}$$

$$T_3 t = m_D (g t - v_{D2}) \quad (2)$$

DISK A:



ANG. MOM. ABOUT O +g:

$$-I_A \omega_{A1} + T_1 t \cdot r_A - T_2 t \cdot r_A = -I_A \omega_{A2}$$

$$T_2 t = T_1 t + \frac{I_A \omega_{A2}}{r_A}$$

$$I_A = \frac{1}{2} M_A r_A^2$$

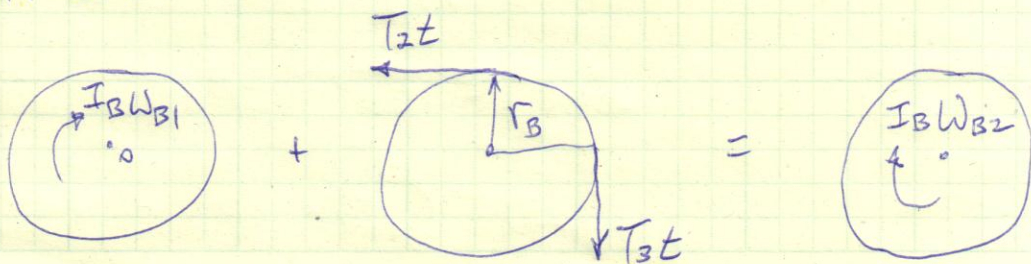
$$T_2 t = M_c (g t + v_{c2}) + \frac{1}{2} M_A r_A \omega_{A2}$$

$$\text{KINEMATICS: } v_{c2} = r_A \omega_{A2}$$

$$T_2 t = M_c (g t + v_{c2}) + \frac{1}{2} M_A v_{c2}$$

$$T_2 t = M_c g t + v_{c2} \left(M_c + \frac{1}{2} M_A \right) \quad (3)$$

DISK B:



ANG. MOM. ABOUT O \uparrow :

$$-I_B \omega_{B1} + T_2 t \cdot r_B - T_3 t \cdot r_B = -I_B \omega_{B2}$$

$$T_2 t = T_3 t - \frac{I_B \omega_{B2}}{r_B}$$

$$I_B = \frac{1}{2} M_B r_B^2$$

$$T_2 t = M_D (g t - v_{D2}) - \frac{1}{2} M_B r_B \omega_{B2}$$

KINEMATICS: $v_{D2} = r_B \omega_{B2} = v_{C2}$

$$T_2 t = M_D g t - v_{C2} (M_D + \frac{1}{2} M_B) \quad (4)$$

SET (3) = (4):

$$M_C g t + v_{C2} (M_C + \frac{1}{2} M_A) = M_D g t - v_{C2} (M_D + \frac{1}{2} M_B)$$

$$g t (M_D - M_C) = v_{C2} (M_C + \frac{1}{2} M_A + M_D + \frac{1}{2} M_B)$$

$$t = \frac{v_{C2}}{g} \cdot \frac{[(M_C + M_D) + \frac{1}{2}(M_A + M_B)]}{(M_D - M_C)}$$

$$t = \frac{(0.5 \frac{m}{s})}{(9.81 \frac{m}{s^2})} \cdot \frac{[(6+10) + \frac{1}{2}(10+6)]}{(10-6)}$$

$$t = 0.3058^s$$