

17.72

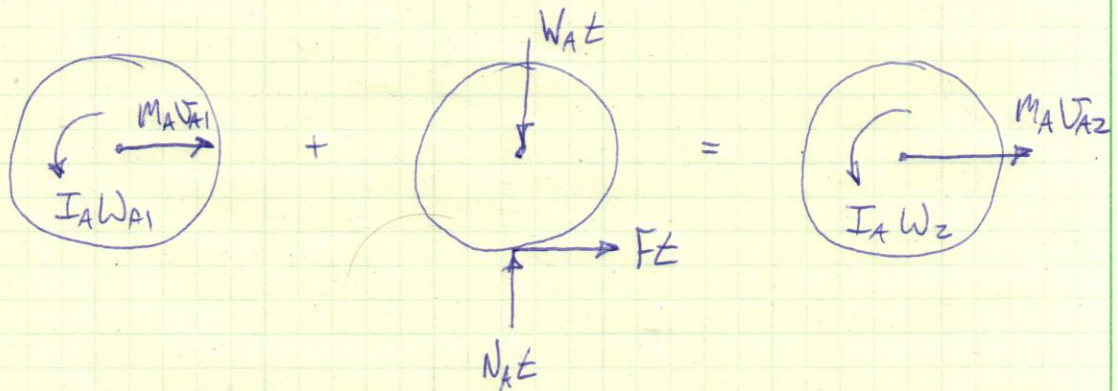
①

$$r = \frac{9}{12} = \frac{3}{4} \text{ ft}, \quad W_A = 18 \text{ lb}, \quad W_B = 6 \text{ lb}, \quad v_{A1} = 0, \quad v_{B1} = 0$$

$$P = 2.5 \text{ lb}, \quad t = 1.2 \text{ s}, \quad \text{FIND } v_A, \quad v_B$$

PRINCIPLE OF IMPULSE AND MOMENTUM:

CYLINDER:



X-DIR. LINEAR MOMENTUM:

$$m_A v_{A1} + Ft = m_A v_{A2}$$

$$Ft = m_A v_{A2} \quad (1)$$

ANGULAR MOMENTUM  $\uparrow$ :

$$I_A \omega_1 + Ft \cdot r = I_A \omega_2$$

$$Ft = \frac{I_A \omega_2}{r}$$

$$I_A = \frac{1}{2} m_A r^2$$

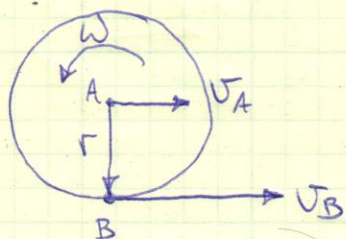
$$Ft = \frac{1}{2} m_A r \omega_2 \quad (2)$$

SET ① = ②:

$$M_A V_{A2} = \frac{1}{2} M_A r \omega_2$$

$$V_{A2} = \frac{1}{2} r \omega_2 \quad (3)$$

KINEMATICS: RELATIVE VELOCITY



$$\vec{V}_B = \vec{V}_A + \vec{V}_{B/A} = \vec{V}_A + \omega \hat{k} \times \vec{r}$$

ALL IN POSITIVE  $\hat{i}$  DIRECTION

$$V_B = V_A + r\omega$$

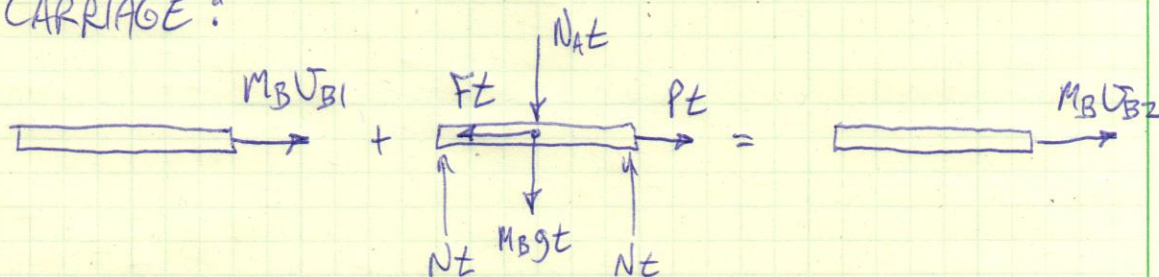
$$\omega_2 = \frac{1}{r} (V_{B2} - V_{A2})$$

USING EQN. ③:

$$V_{A2} = \frac{1}{2} r \left[ \frac{1}{r} (V_{B2} - V_{A2}) \right]$$

$$V_{A2} = \frac{1}{3} V_{B2} \quad (4)$$

CARRIAGE:



X-DIR. LIN. MOM.:

$$M_B V_{B1} - Fz + Pt = M_B V_{B2}$$

USE EQN. ①:

$$-(M_A V_{A2}) + Pt = M_B V_{B2}$$

USE EQN. ④:

$$-M_A \left( \frac{1}{3} V_{B2} \right) + Pt = M_B V_{B2}$$

$$V_{B2} = \left( \frac{3}{3M_B + M_A} \right) \cdot Pt \quad W = mg, \quad m = \frac{W}{g}$$

$$V_{B2} = \left( \frac{3g}{3W_B + W_A} \right) \cdot Pt$$

$$V_{B2} = \left[ \frac{3(32.2 \frac{\text{ft}}{\text{s}^2})}{3(6 \text{ LB}) + (18 \text{ LB})} \right] \cdot (2.5 \text{ LB}) (1.2 \text{ s})$$

$$V_{B2} = 8.05 \frac{\text{ft}}{\text{s}}$$

$$V_{A2} = \frac{1}{3} (8.05) = 2.683 \frac{\text{ft}}{\text{s}}$$