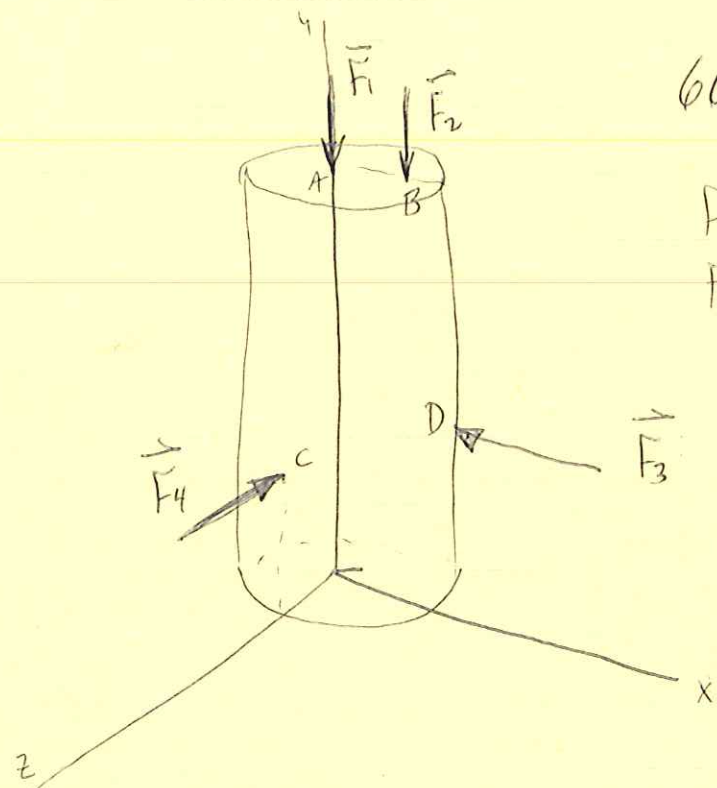


EXAMPLE PROB. 3,119



60-mm-dia cylinder

Find EQUIVALENT
FORCE-COUPLE SYSTEM
AT C

~~A(0, 140, 0)~~
~~A(0, 140, 0)~~
A(0, 140, 0)
B(20, 140, 0)
C(0, 30, 30)
D(30, 60, 0)

$$\vec{R} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \vec{F}_4$$

$$\vec{M}_C = \vec{r}_{CA} \times \vec{F}_1 + \vec{r}_{CB} \times \vec{F}_2 + \vec{r}_{CD} \times \vec{F}_3$$

FORCES: ~~FOR F1~~ $\vec{F}_1 = (-17)\hat{j}$ N

$$\vec{F}_2 = (-12)\hat{j}$$
 N

$$\vec{F}_3 = (-21)\hat{i}$$
 N

$$\vec{F}_4 = (-16)\hat{k}$$
 N

$$\vec{R} = (-21)\hat{i} + (-29)\hat{j} + (-16)\hat{k}$$
 N

FIND POSITION VECTORS.

FOR \vec{r}_{CA} :

~~COORDINATES OF POINT C: $X_C = 0$, $Y_C = 30$ mm, $Z_C = 30$ mm~~

~~POINT A: $X_A = 0$, $Y_A = 140$ mm, $Z_A = 0$~~

$$dx = X_A - X_C = 0 - 0 = 0$$

$$dy = Y_A - Y_C = 140 - 30 = 110 \text{ mm}$$

$$dz = Z_A - Z_C = 0 - 30 = -30 \text{ mm}$$

$$d = \sqrt{110^2 + 30^2} = 114.0 \text{ mm}$$

$$\vec{r}_{CA} = (0)\hat{i} + (110)\hat{j} + (-30)\hat{k} \text{ mm}$$

FOR \vec{r}_{CB} :

~~POINT B: $X_B = 20$ mm, $Y_B = 140$ mm, $Z_B = 0$~~

$$dx = X_B - X_C = 20 - 0 = 20 \text{ mm}$$

$$dy = Y_B - Y_C = 140 - 30 = 110 \text{ mm}$$

$$dz = Z_B - Z_C = 0 - 30 = -30 \text{ mm}$$

$$\vec{r}_{CB} = (20)\hat{i} + (110)\hat{j} + (-30)\hat{k} \text{ mm}$$

FOR \vec{r}_{CD} :

PROB. 3.119 CONT.

~~POINT D: $x_D = 0$, $y_D = 60$ mm, $z_D = 0$~~

~~$d_x = x_D - x_C = 30 - 0 = 30$ mm~~

~~$d_y = y_D - y_C = 60 - 30 = 30$ mm~~

~~$d_z = z_D - z_C = 0 - 30 = -30$ mm~~

~~$\vec{r}_{CD} = (30)\hat{i} + (30)\hat{j} + (-30)\hat{k}$ mm~~

~~$\vec{M}_C = \vec{r}_{CA} \times \vec{F}_1 + \vec{r}_{CB} \times \vec{F}_2 + \vec{r}_{CD} \times \vec{F}_3 = \vec{M}_1 + \vec{M}_2 + \vec{M}_3$~~

~~$M_1 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 110 & -30 \\ 0 & -17 & 0 \end{vmatrix}$~~

~~$\vec{M}_1 = [(110)(0) - (-30)(-17)]\hat{i}$~~

~~$- [(0)(0) - (-30)(0)]\hat{j}$~~

~~$+ [(0)(-17) - (110)(0)]\hat{k}$~~

~~$\vec{M}_1 = (-510)\hat{i}$ N-mm~~

~~$\vec{M}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 20 & 110 & -30 \\ 0 & -12 & 0 \end{vmatrix}$~~

$$\begin{aligned}\vec{M}_2 &= [(110 \times 0) - (-30 \times -12)] \hat{i} \\ &\quad - [(20 \times 0) - (-30 \times 0)] \hat{j} \\ &\quad + [(20 \times -12) - (110 \times 0)] \hat{k}\end{aligned}$$

$$\vec{M}_2 = (-360) \hat{i} + (0) \hat{j} + (-240) \hat{k} \quad \text{N-mm}$$

$$\vec{M}_3 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 30 & 30 & -30 \\ -21 & 0 & 0 \end{vmatrix}$$

$$\begin{aligned}\vec{M}_3 &= [(30 \times 0) - (-30 \times 0)] \hat{i} \\ &\quad - [(30 \times 0) - (-30 \times -21)] \hat{j} \\ &\quad + [(30 \times 0) - (30 \times -21)] \hat{k}\end{aligned}$$

$$\vec{M}_3 = (0) \hat{i} + (630) \hat{j} + (630) \hat{k} \quad \text{N-mm}$$

$$\begin{aligned}\vec{M}_c &= (-510) \hat{i} + (-360) \hat{i} + (-240) \hat{k} \\ &\quad + (630) \hat{j} + (630) \hat{k} \quad \text{N-mm}\end{aligned}$$

$$\vec{M}_c = (-870) \hat{i} + (630) \hat{j} + (390) \hat{k} \quad \text{N-mm}$$

$$\vec{M}_c = (-0.87) \hat{i} + (0.63) \hat{j} + (0.39) \hat{k} \quad \text{N-m}$$